

# Radio wavefront shape of cosmic ray air showers



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for the LOFAR Key Science Project Cosmic Rays

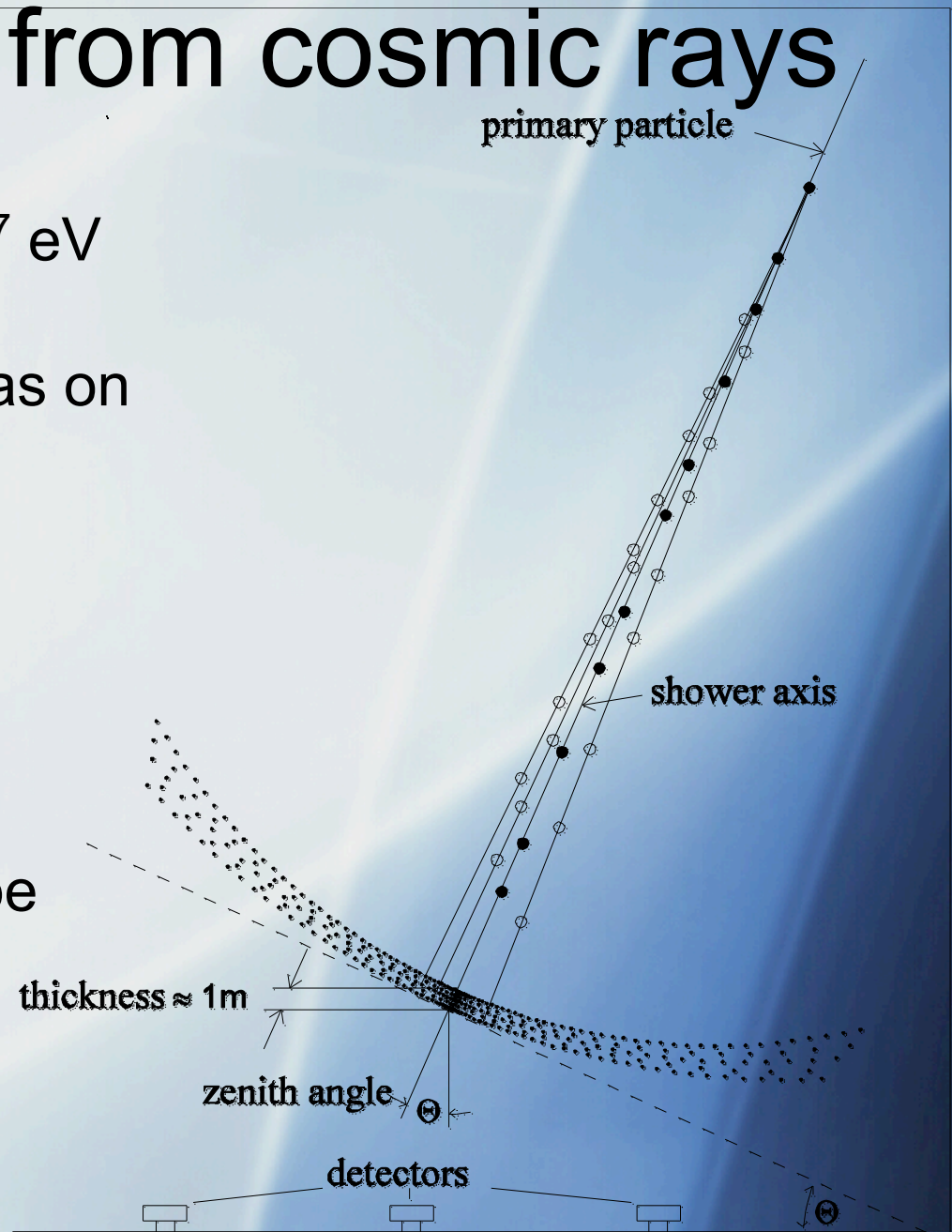
LOFAR Community Science Workshop, April 9, 2014

# Radio pulses from cosmic rays

Short (10 ns) pulses from cosmic-ray particles  $> \sim 10^{17}$  eV

In 200 - 400 LOFAR antennas on the ground, we measure:

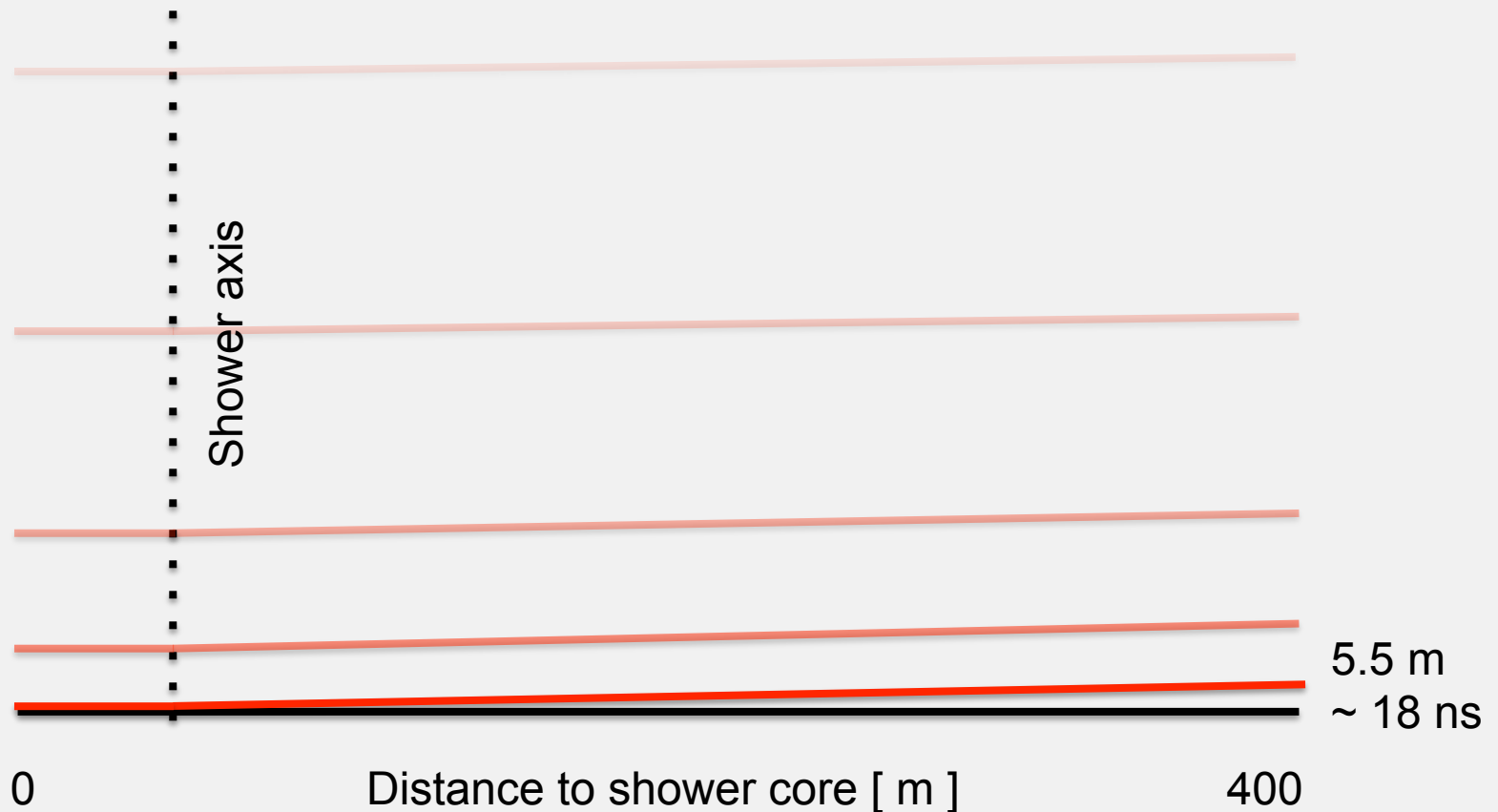
- Lateral distribution of
  - Signal power
  - Signal arrival time
    - Wavefront shape
  - Spectrum / pulse shape
  - Polarization
- Wavefront shape measurements



# Wavefront at actual aspect ratio

Snapshot at the moment wavefront touches ground

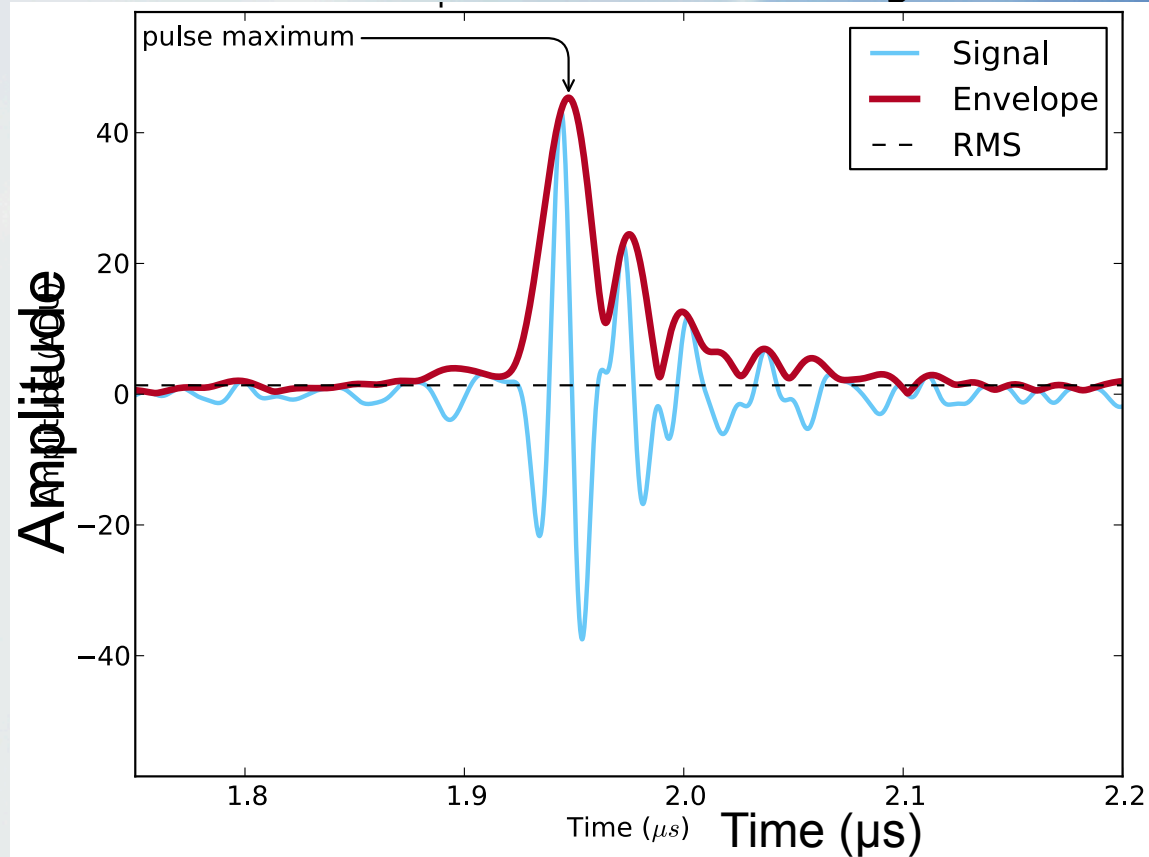
Angle with shower plane  $\sim 0.8^\circ$



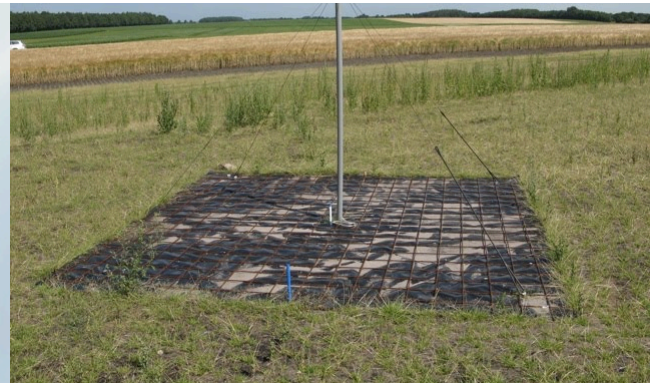
# Arrival times for a cosmic ray

Measuring arrival time of pulse in individual antennas:

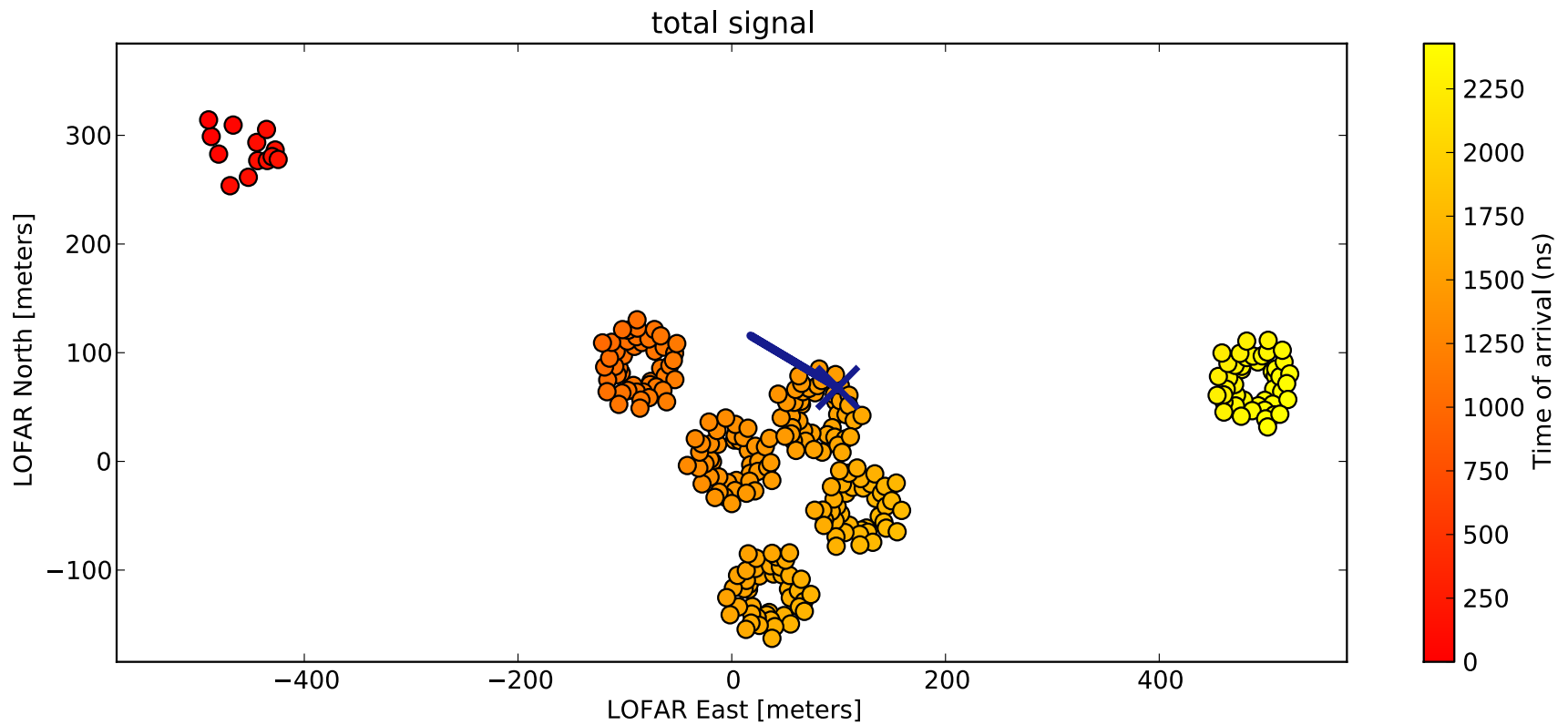
- Time series signal  
Apply Hilbert transform to get *Hilbert envelope*
- Envelope maximum is 'the arrival time'



$$\sigma_t = \frac{12.7}{SNR} \text{ ns} < 5 \text{ ns!}$$

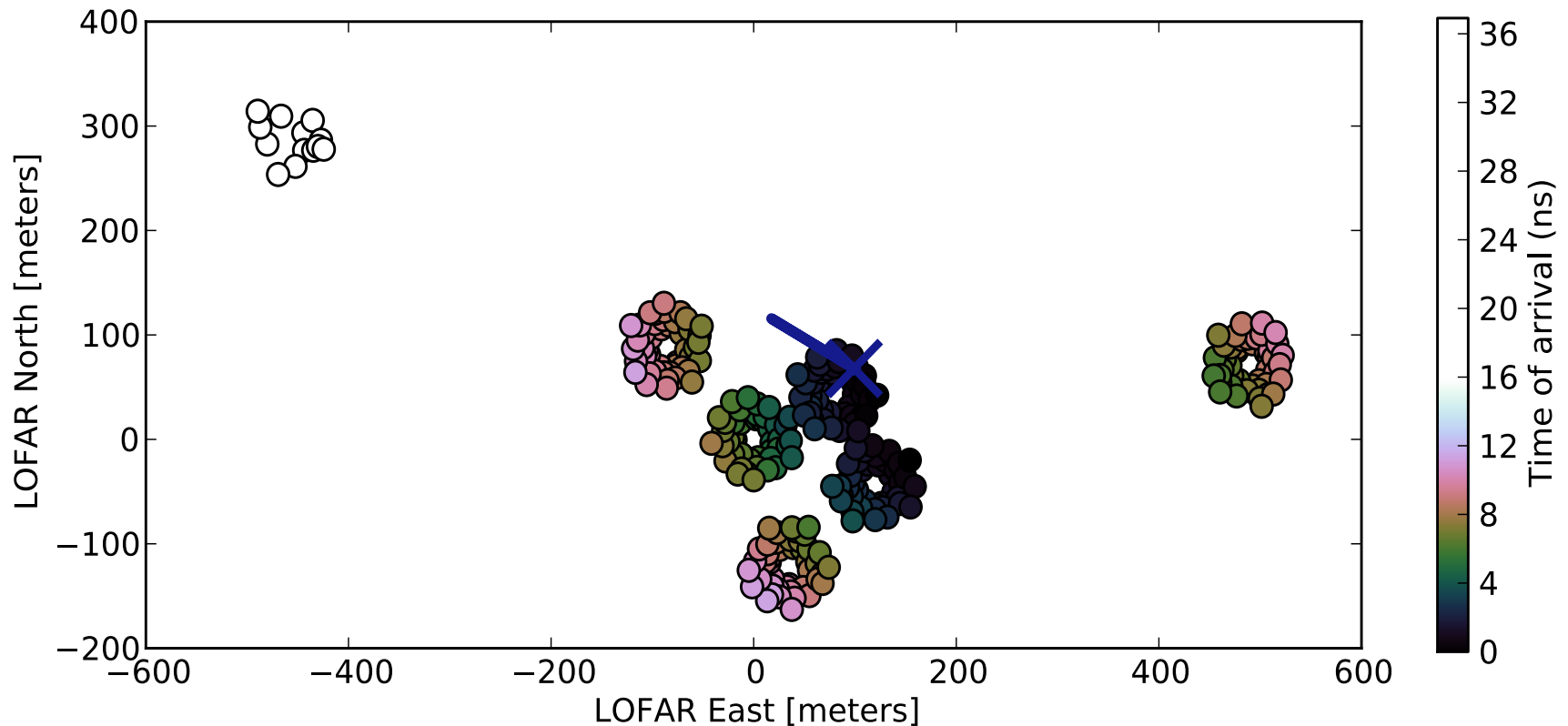


# Arrival times for a cosmic ray



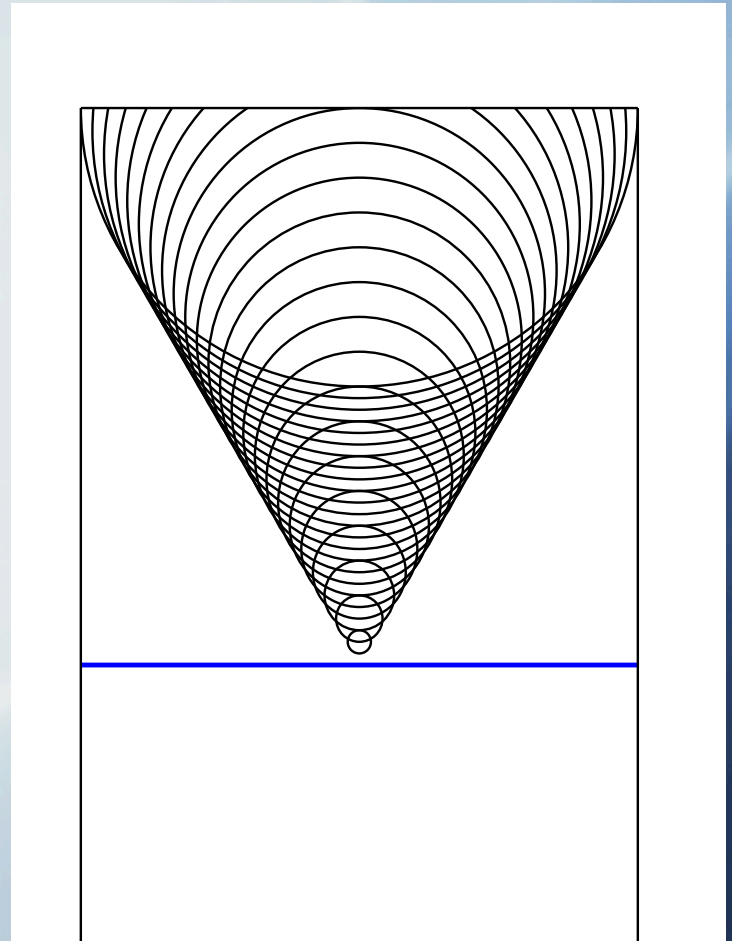
# Arrival times after subtracting plane-wave solution

Corstanje et al., to be submitted to Astroparticle Physics



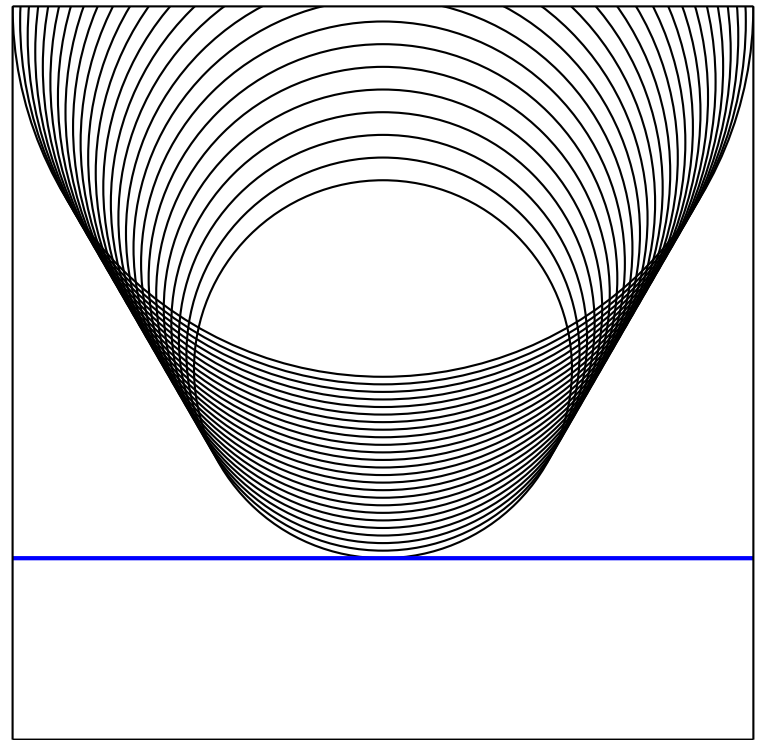
# Toy model for wavefront shape

- A point source moving at  $v = c$
- Emitting radiation for a limited time
- Medium has refractive index  $n$
- Waves propagate at  $v = c/n$
- Emission all the way to the ground: **conical** shape



# Toy model for wavefront shape

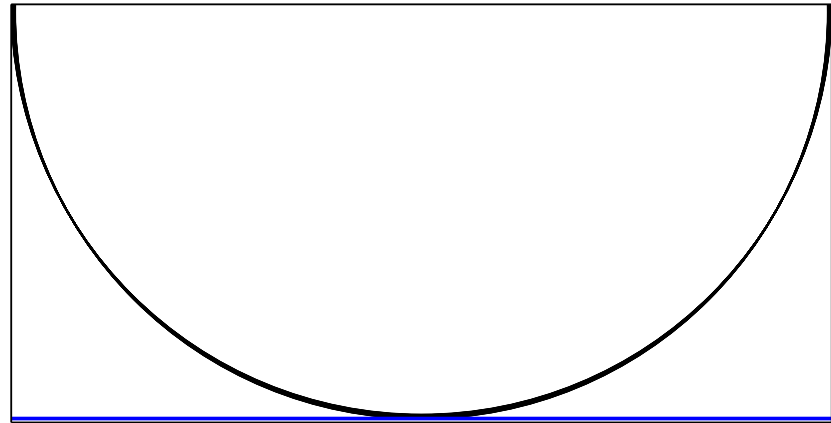
- A point source moving at  $v = c$
- Emitting radiation for a limited time
- Medium has refractive index  $n$
- Waves propagate at  $v = c/n$
- Emission stops before ground:  
**hyperbolic**(-like) shape



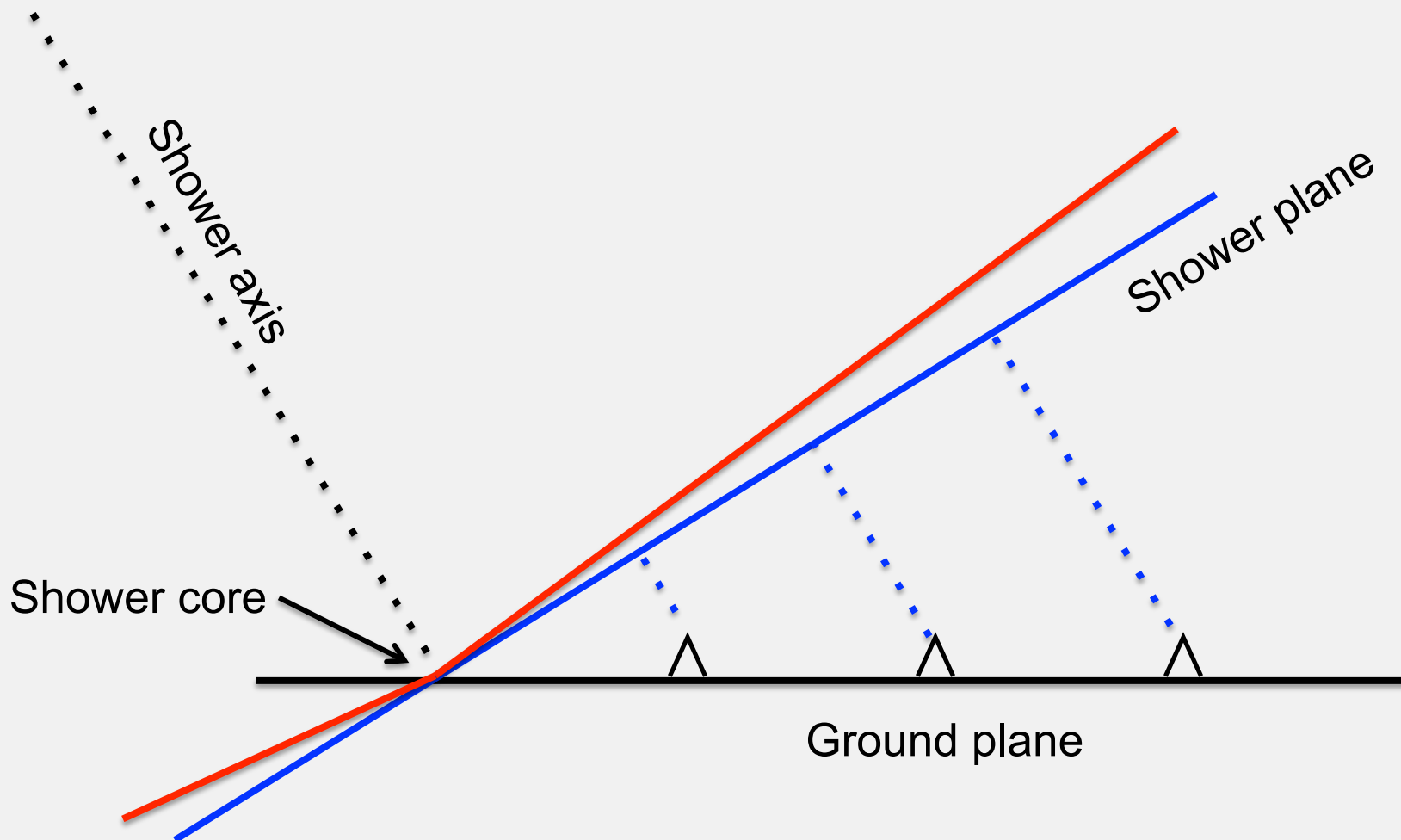


# Toy model for wavefront shape

- A point source moving at  $v = c$
- Emitting radiation for a limited time
- Medium has refractive index  $n$
- Waves propagate at  $v = c/n$
- Emission only very far from ground: **spherical** shape



# Shower plane projection

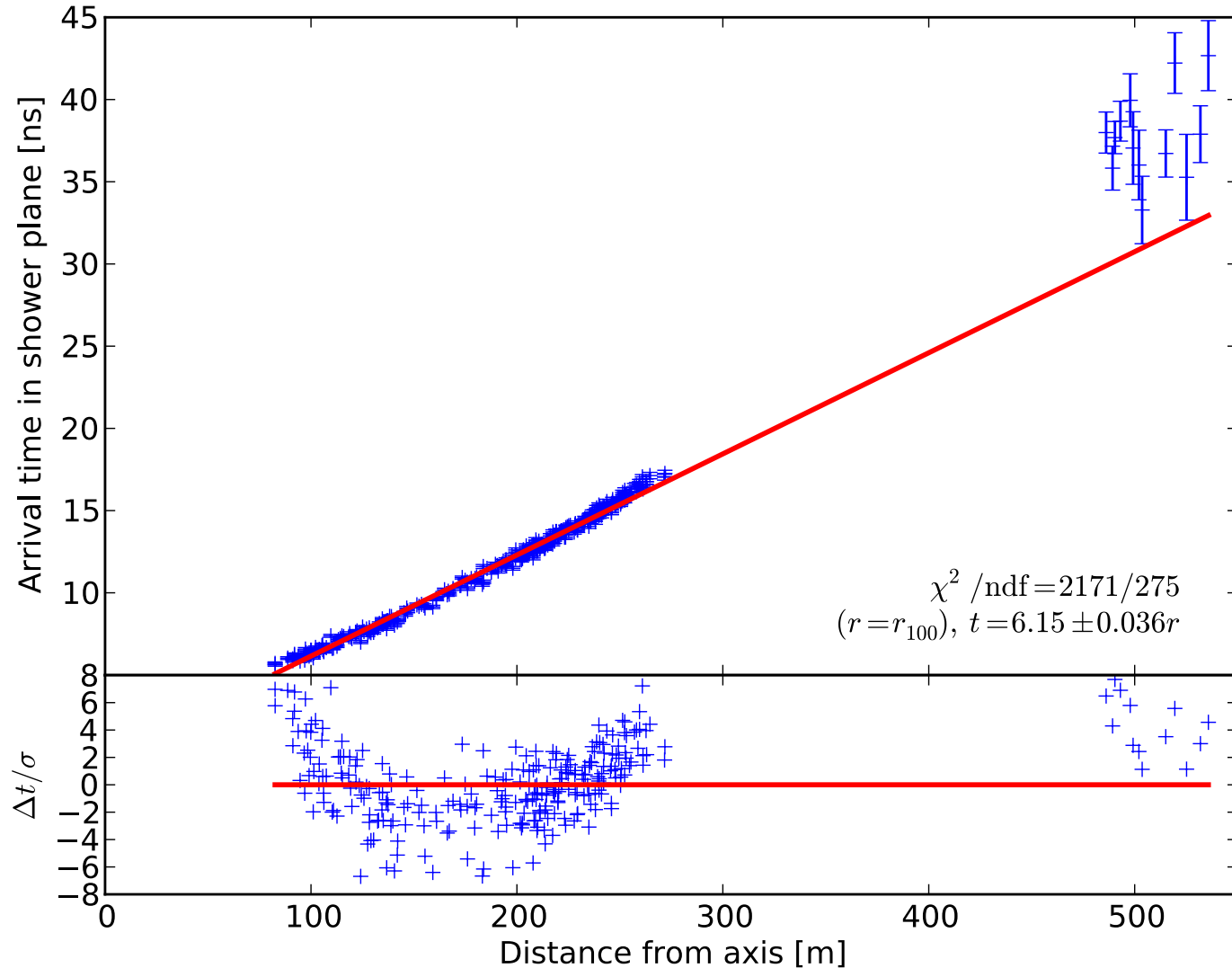


# Shower plane

- Project antennas into shower plane
  - Shower axis position
  - Shower axis direction
  - Unknown: free **fit parameters**
- Wavefront: arrival times as function of distance from shower axis
- Nested fitting (7 params):
- Optimize shower **core position**
  - Optimize axis **direction**
    - Optimize **curve-fit**

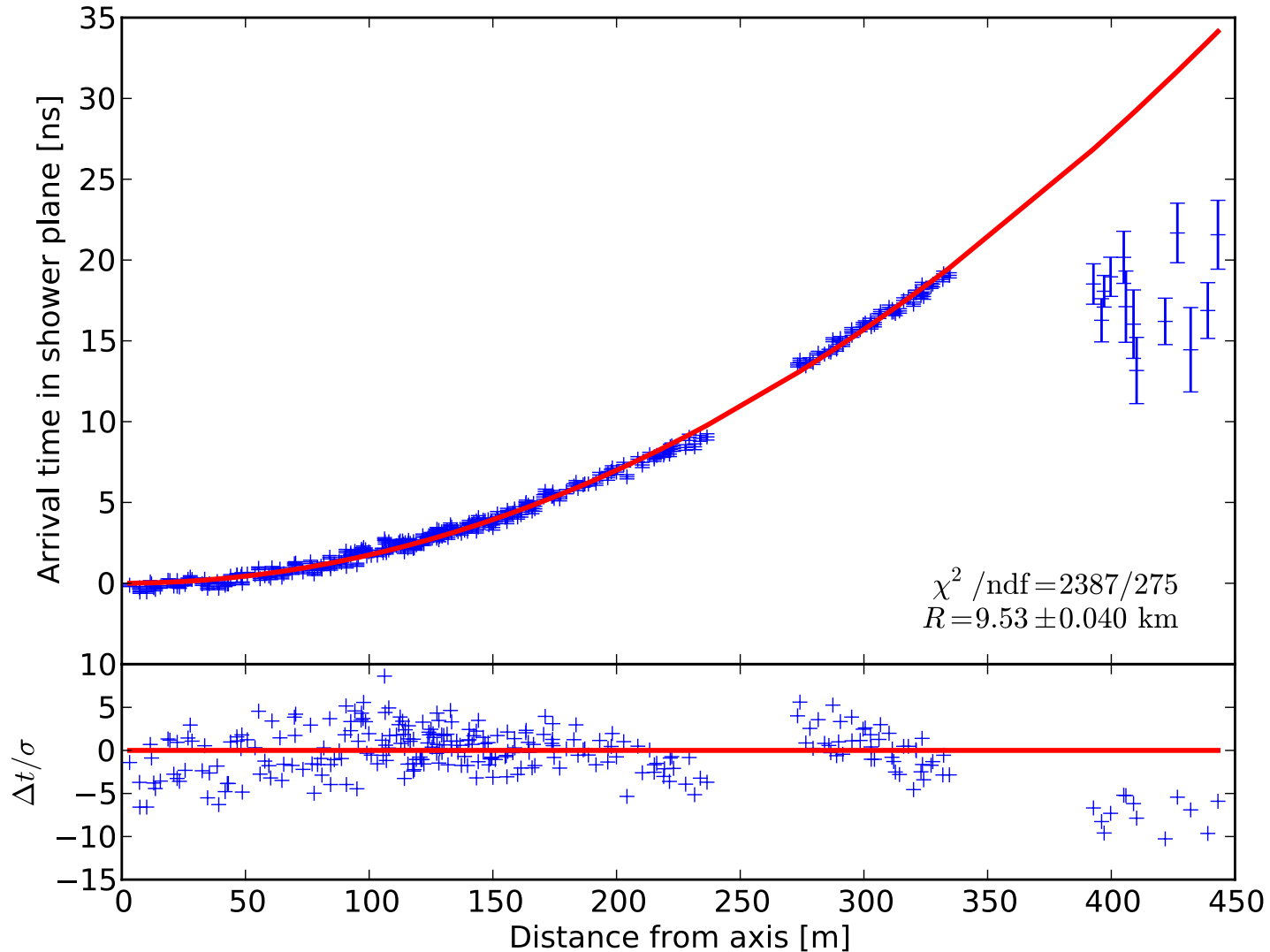
# Best-fitting conical shape

Corstanje et al., to be submitted to Astroparticle Physics



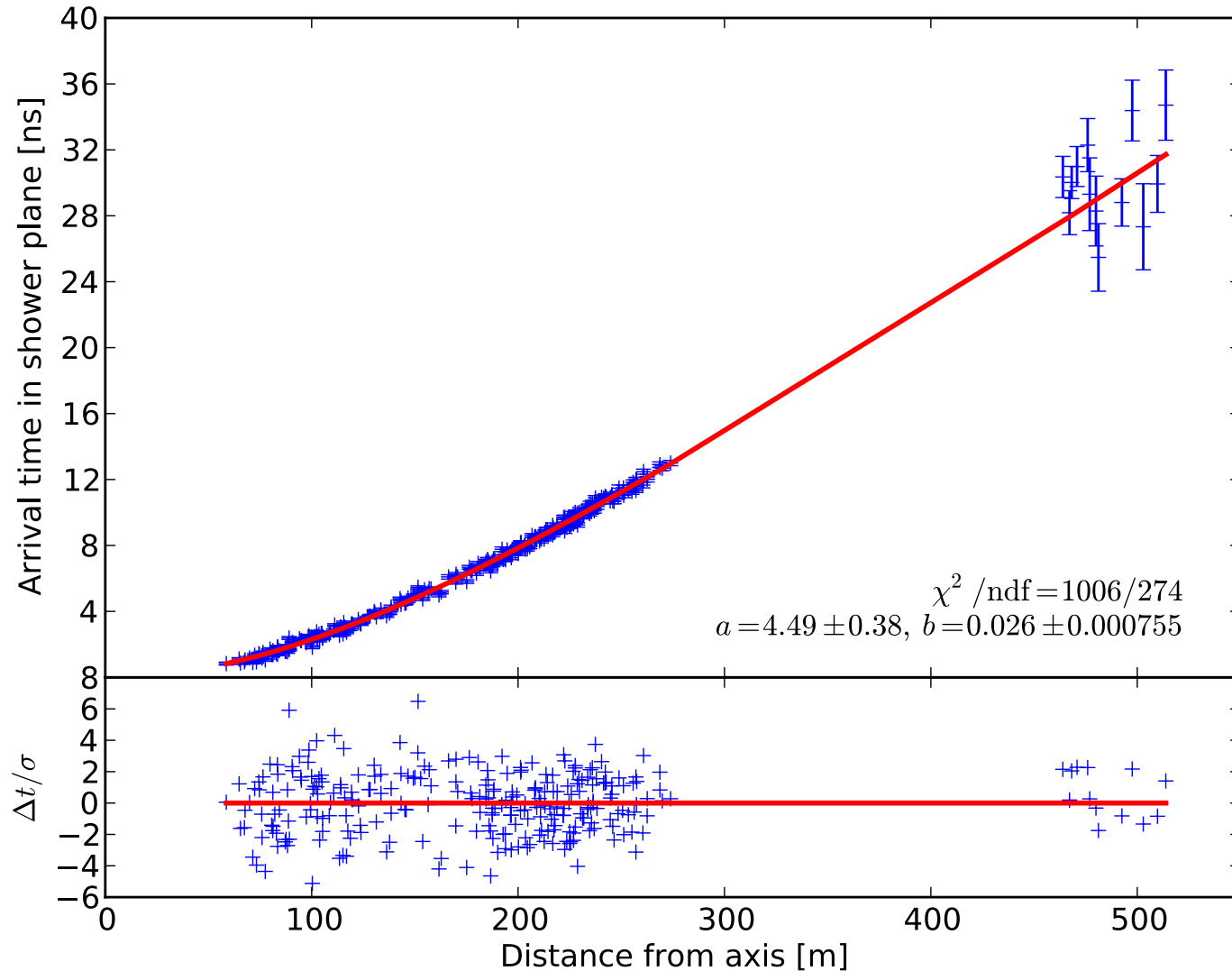
# Best-fitting spherical shape

Corstanje et al., to be submitted to Astroparticle Physics

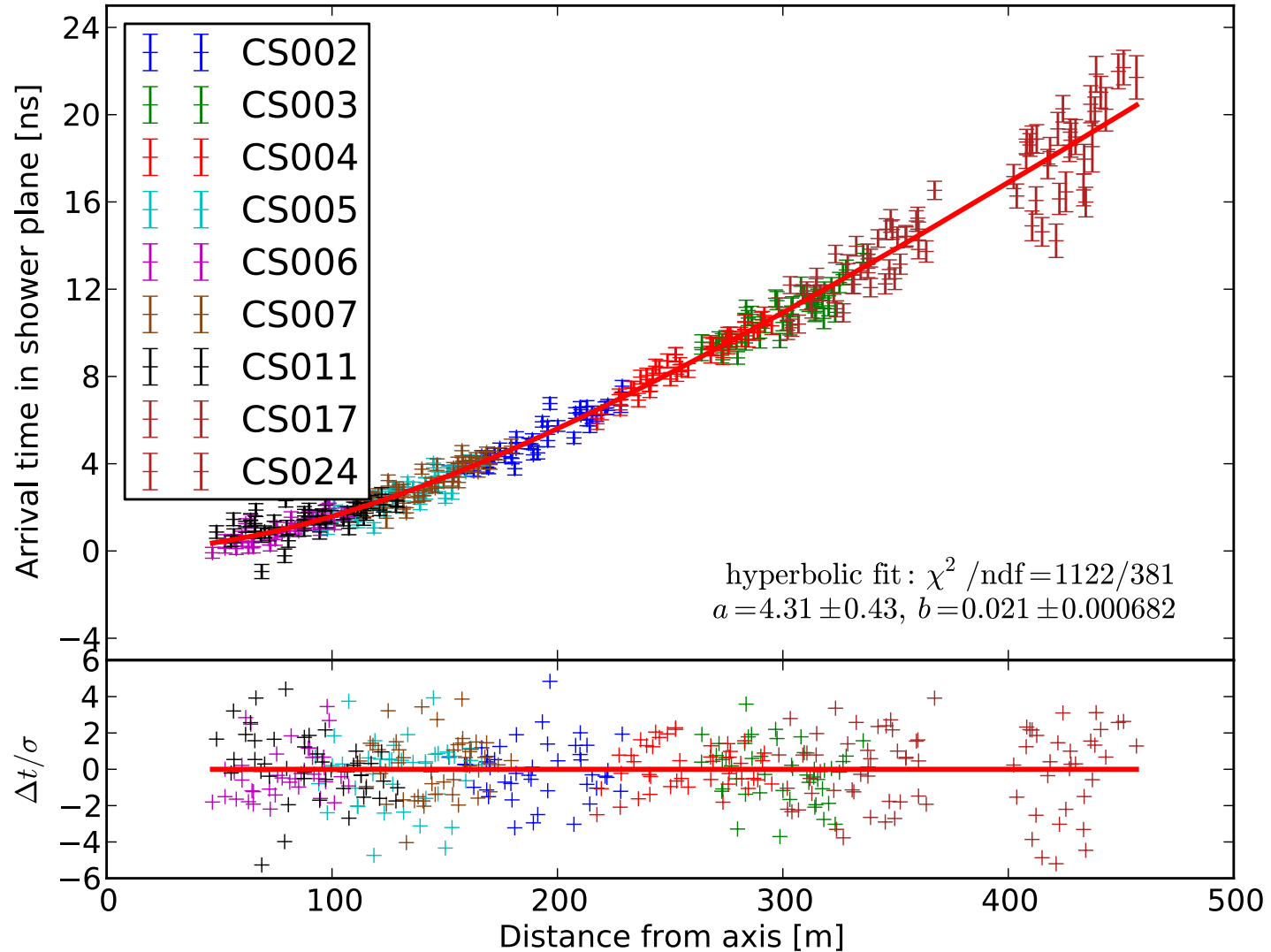


# Best-fitting hyperbolic shape

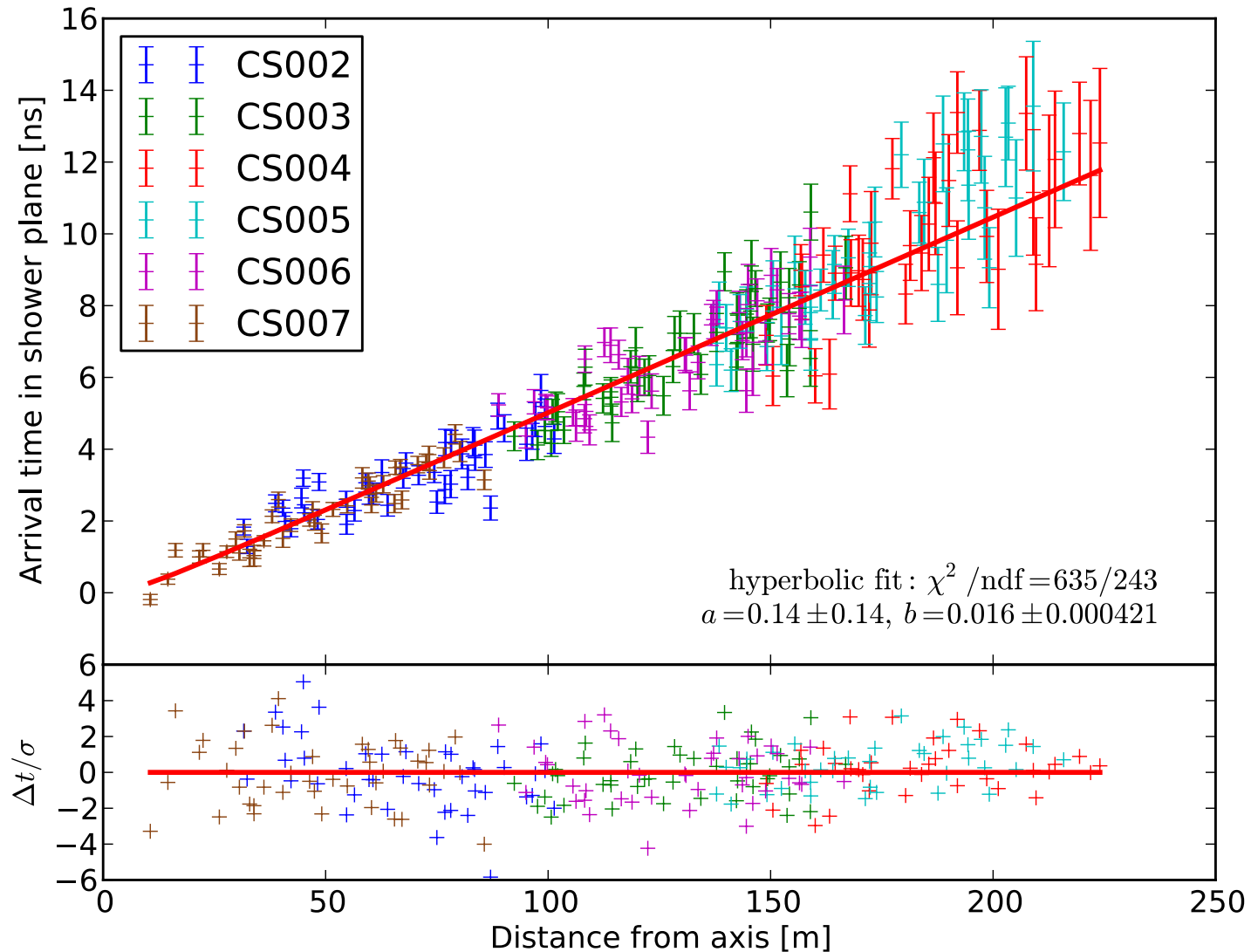
Corstanje et al., to be submitted to Astroparticle Physics



# Another example



# Conical-shaped example

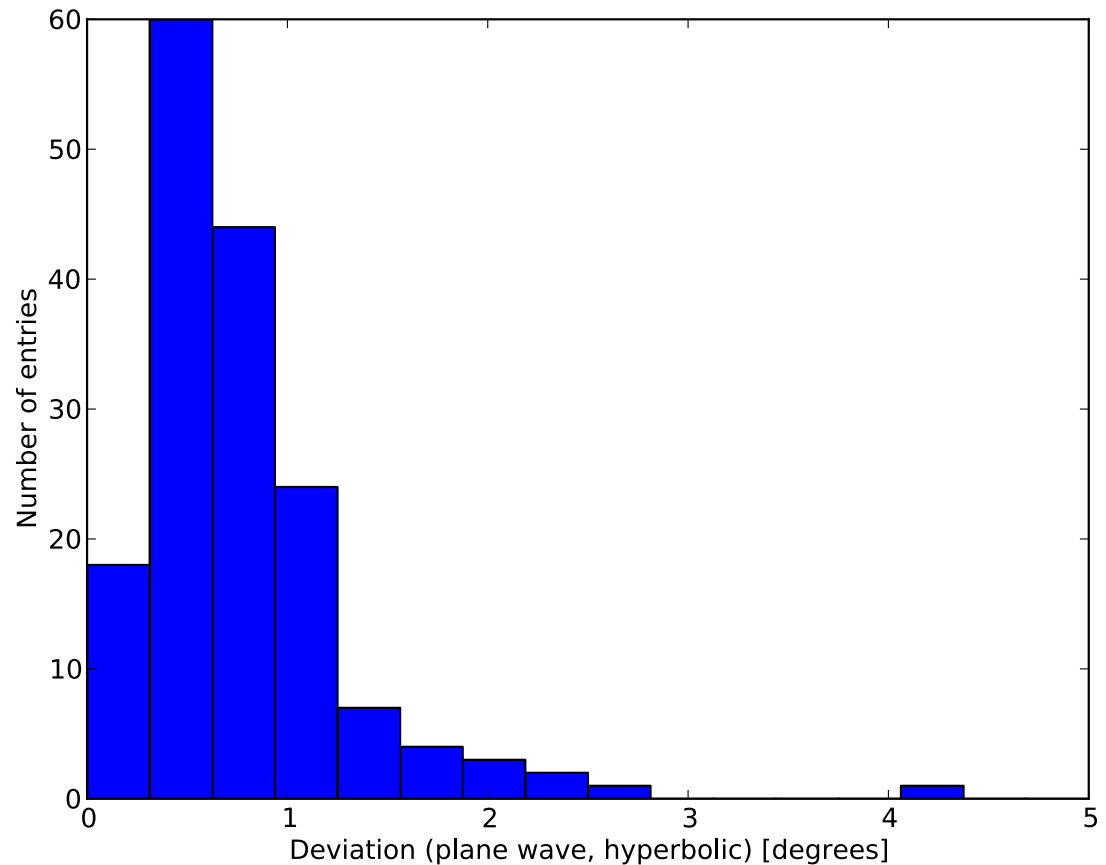




# Improved angular resolution

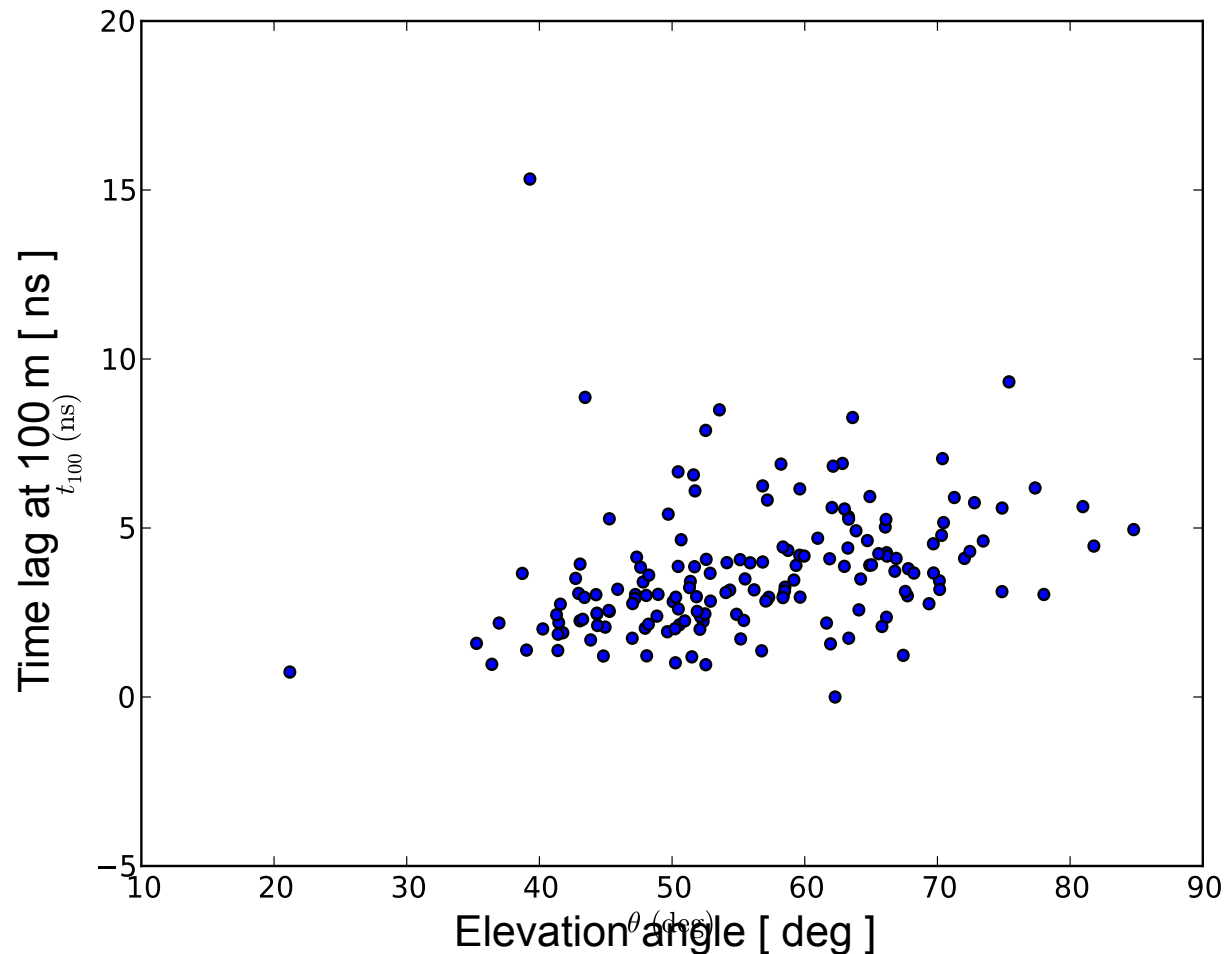
Corstanje et al., to be submitted to Astroparticle Physics

- Using hyperbolic wavefront improves directional accuracy
- About 1 degree difference
- Difference with conical shape  $\sim 0.1$  degree



# Elevation angle dependence

- Time lag at 100 m from shower axis of best-fitting hyperboloid
- Weak correlation with elevation angle
- Uncertainty in shower core position



# Conclusions and outlook

- Wavefront timing measured with accuracy better than 1 ns per antenna
- A hyperboloid clearly fits best; no significant structure in residuals
  - Significant spread between events, well resolved
- Arrival direction more accurately fitted using hyperboloid wavefront (to  $\sim 0.1$  deg)
- Compare with simulations to get more accurate shower core position, and correlate with  $X_{\max}$  and particle type